

Classification of Fingerprints

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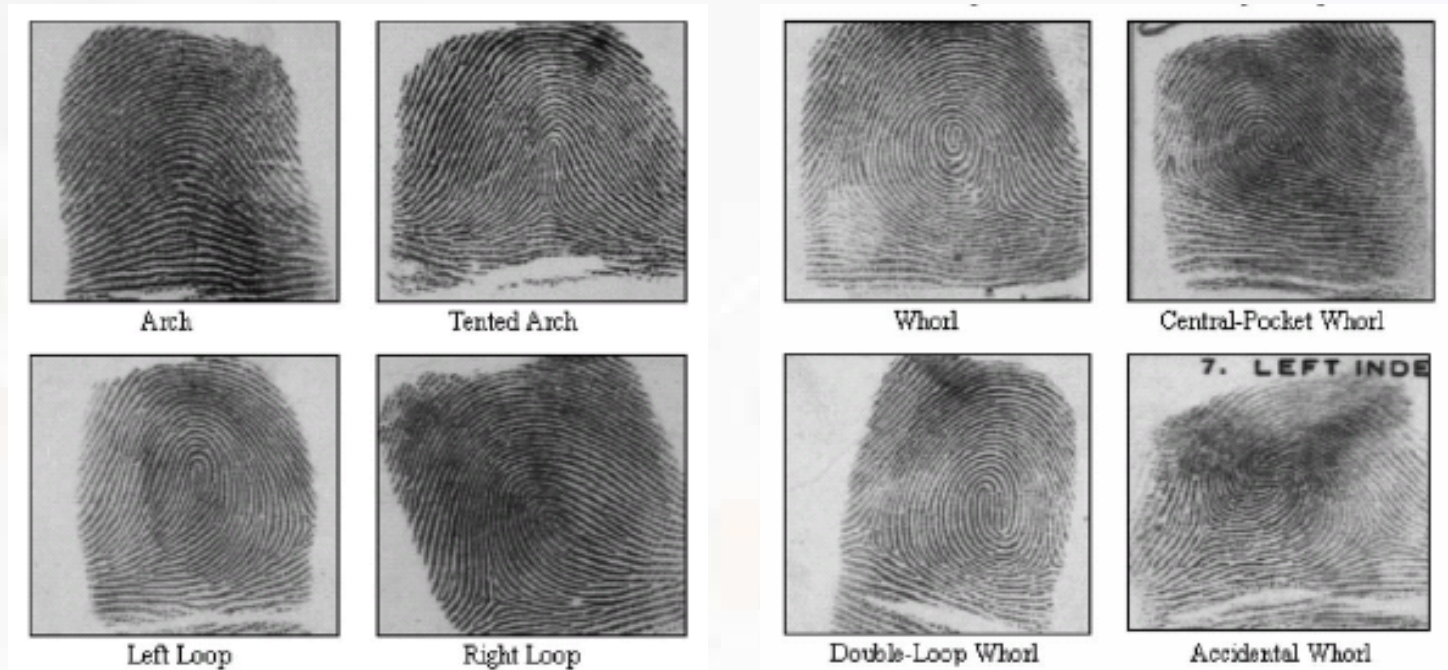
Fingerprint Classification

- ✦ Fingerprint classification is a coarse level partitioning of a fingerprint database into smaller subsets.
- ✦ Fingerprint classification reduces the search space of a large database: Determine the class of the query fingerprint. Then, only search templates with the same class as the query.
- ✦ Illustration: Inputs are the fingerprint impressions from 10 fingers of an individual. If size of the database is N and D is the number of classes,

Search space without classification: N^{10}

Search space with classification: $(N/D)^{10}$

The Henry Classification System



- Henry (1900) made an extensive study of occurrence of fingerprints and indexed them into 8 major classes.
- The 8 classes are shown above. The four different whorl classes can be combined into one class: Whorl (W).

The Henry Classification System (cont.)



Left-loop (LL)



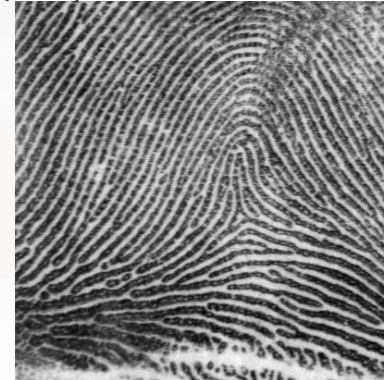
Right-loop (RL)



Whorl (W)



Plain Arch (PA)



Tented Arch (TA)

The Henry system with five classes are shown above. The five classes can be reduced to four by combining the PA and TA classes to form the Arch (A) class. The natural frequencies of W, L, R and A (A + T) are 27.9%, 33.8%, 31.7% and 6.6%.

The Henry Classification System (cont.)

- The five main classes differ in terms of the global flow patterns of the ridge curves.
- They also differ in terms of the number and locations of singular points in the fingerprint image. For example,
 - LL – exactly one core and one delta; the core is to the left of the delta,
 - RL – exactly one core and one delta; the core is to the right of the delta,
 - W – two cores and two deltas,
 - PA – no singular points, and
 - TA – one core and one delta; the delta is approximately directly below the core.

Problems with the Henry classification system: (i) non-uniform classification proportions, and (ii) experts classify some fingerprint images into different Henry classes.

Examples of such fingerprints are...



TA and LL



TA and RL



TA and PA

Approaches for Fingerprint Classification

- ✦ Approaches based on **singular points**: Hong and Jain (1999), Karu and Jain (1996).
- ✦ **Structure-based** approaches such as using the orientation field and geometry of ridges: Cappelli et. al (2002), Chang & Fan (2002), and Chong et. al (1997).
- ✦ **Frequency-based** approaches using Fourier spectrum: Jain et. al (1999).
- ✦ **Syntactic or grammar-based**: Moayer & Fu (1975,1976).
- ✦ **Mathematical models**: Silviu & Jain (2002), Dass & Jain (2004).
- ✦ **Hybrid methods**: Combination of at least two of the above approaches (Chang & Fan (2002) and Chong et. al (1997))

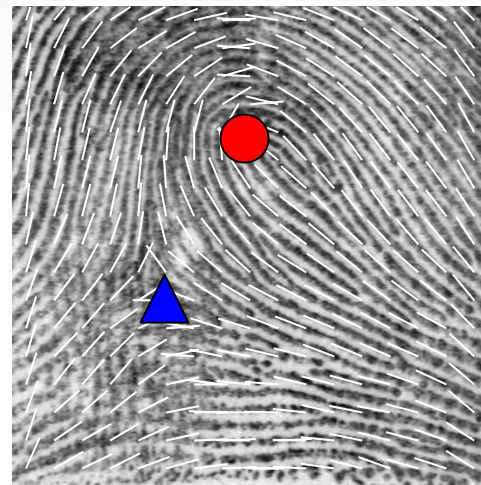
Singular point based approaches

Karu and Jain (1996) classifies fingerprints by detecting singular points in the fingerprint image.

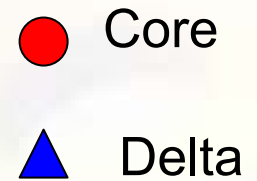
1. The orientation field (flow direction of the ridges at each site in the fingerprint image) is extracted and smoothed.
2. Singular points are detected using the Poincare index. The Poincare index is computed by summing the changes in the angles of flow in a small circle around the test point. It is 0 , $-\pi$, π , and 2π for regular, delta, core and double core points, respectively.



Input image

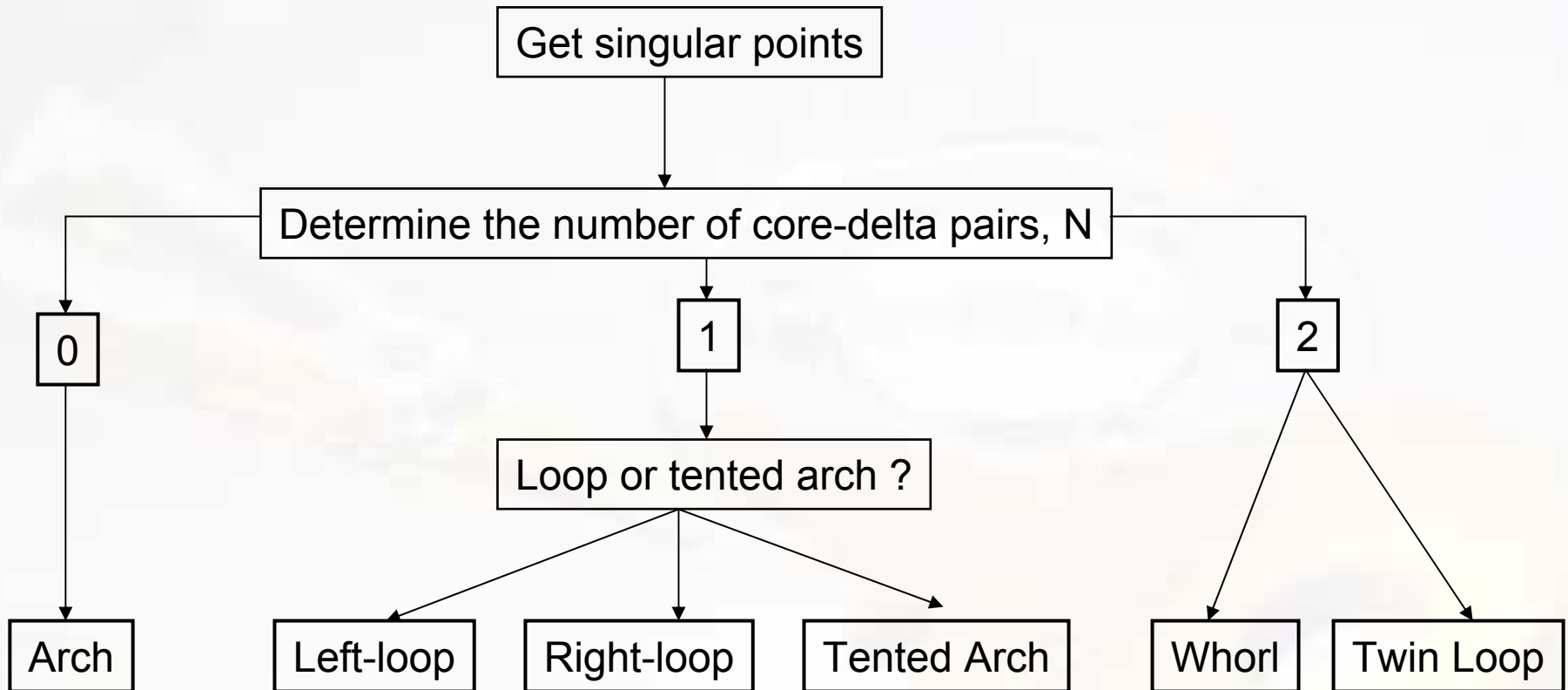


Orientation Field



Karu and Jain (1996), cont.

The classification procedure is:

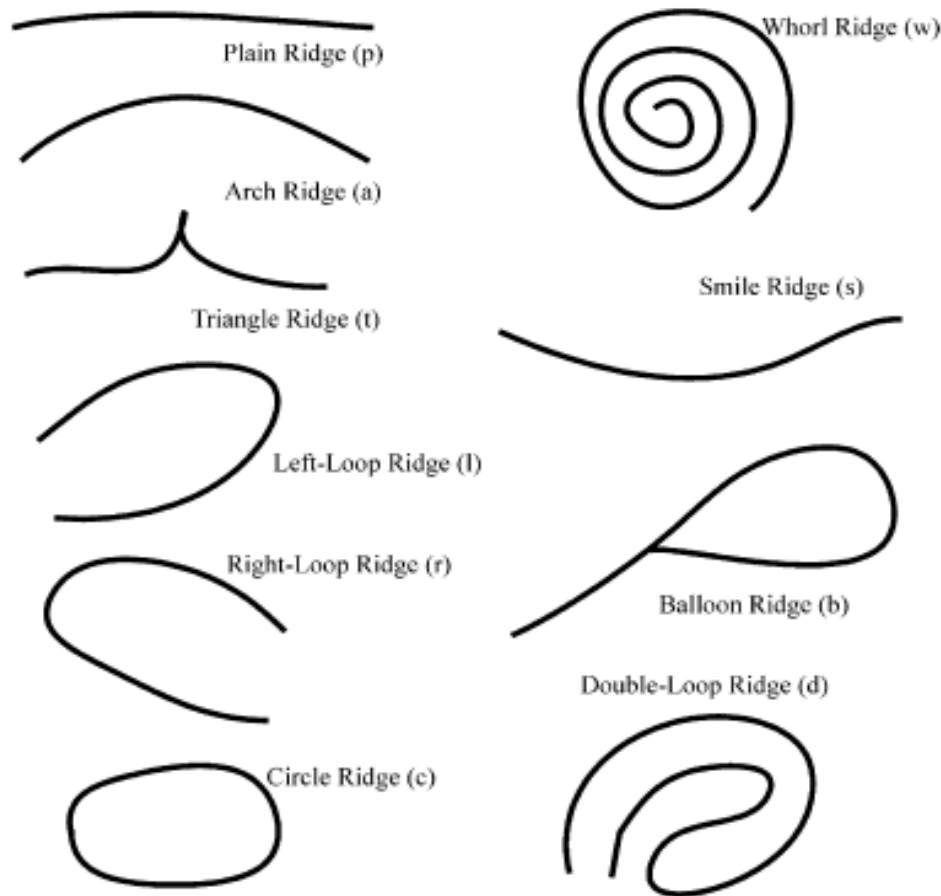


1. If $N=1$, consider the straight line joining the core and the delta. If $N=2$, consider the straight line joining the two cores. Call this line L .
2. For tented arch (whorl), the tangent direction of L is parallel to the local orientation values, but not so for loops (twin loop).

Structure based approaches

Structure based approaches use global characteristics of the ridges to determine the fingerprint class.

Chang & Fan (2002) use ridge distribution models to determine the class of the fingerprint.

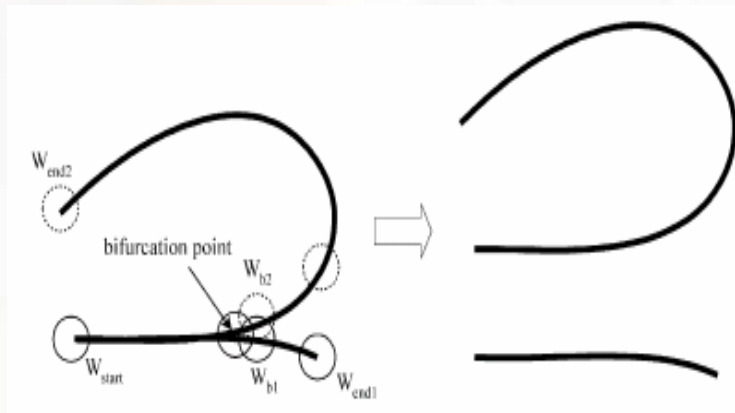


The 10 basic ridge patterns of Chang & Fan are given on the left.

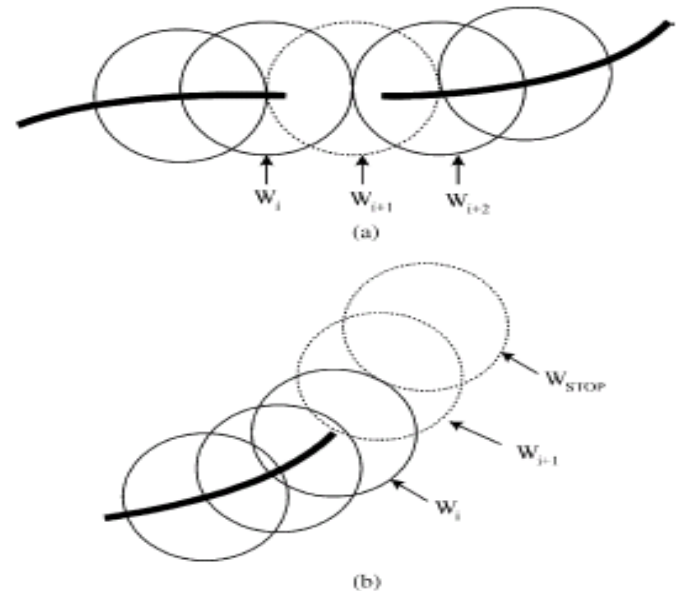
Chang & Fan (2002)

The fingerprint classification procedure is based on the following steps:

1. For a given fingerprint image, an algorithm for extracting the ridges is developed. This algorithm takes into account (i) ridge bifurcations, and (ii) ridge fragmentations which are not endings.



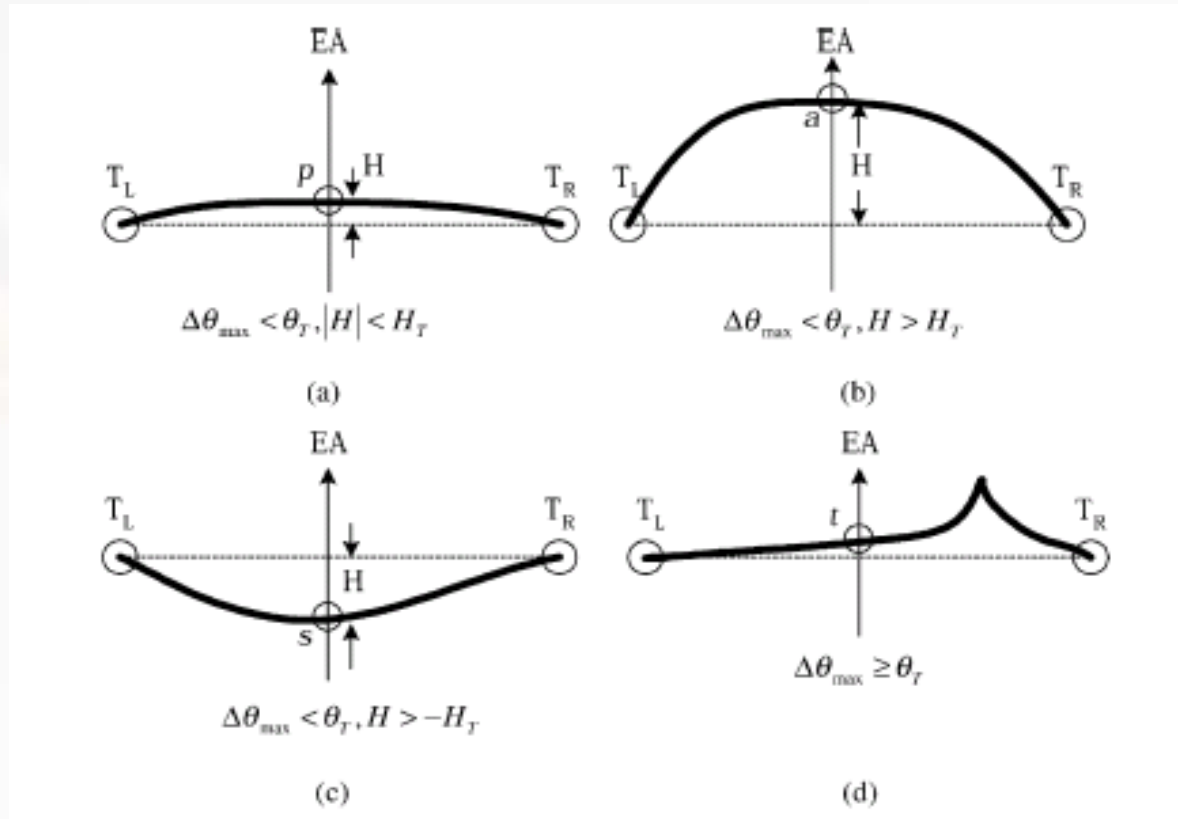
(i) Handling ridge bifurcations



(i) Handling ridge fragmentations (a), true ridge endings (b).

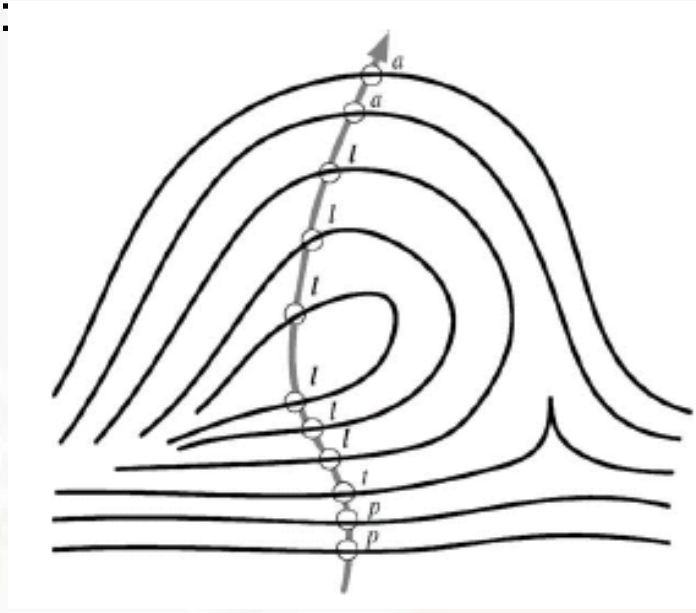
Chang & Fan (2002), cont.

2. Each extracted ridge is then classified into one of the 10 basic ridge patterns. Some examples of the classification are:



Chang & Fan (2002), cont.

3. The ridge distribution sequence is generated according to the picture below:



- Each of the 7 classes of the Henry system (except the accidental whorl) has a unique ridge distribution sequence associated to it.
- Fingerprint images whose ridge distribution sequence cannot be determined are rejected.
- The accidental whorl class is a subset of the rejected images.
- Experimental results with the NIST4 database: 93.4% with 5.1% rejection rate for 7 classes, and 94.4% for the 5 classes.

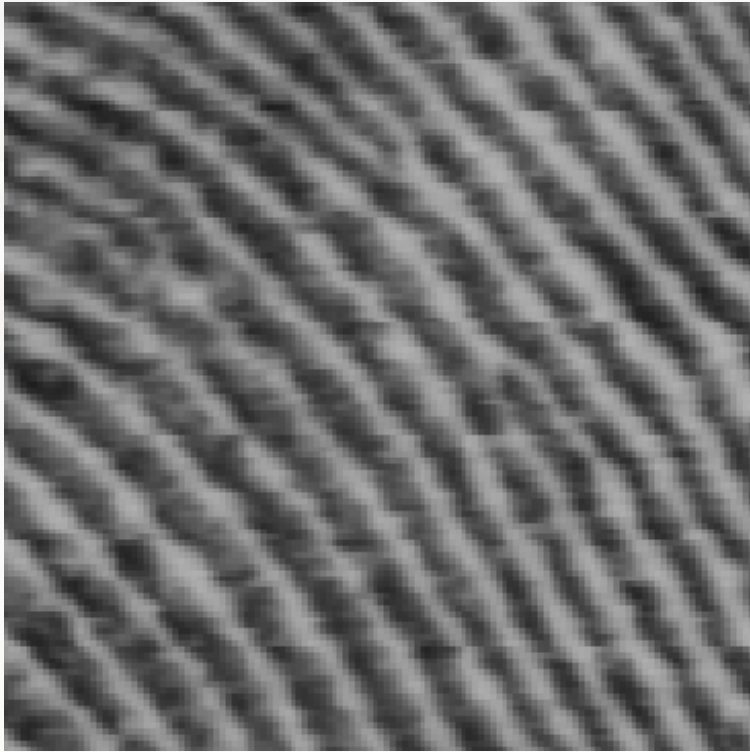
Structural based approach - Chong & Ngee (1997)

1. The fingerprint classification procedure is based on determining the global geometric structure of the extracted ridges using B-splines.
2. The B-splines provide a compact representation of the ridges and contain enough information to determine their geometric structure.
3. The main drawback of this method is that it was not tested on a large number of fingerprints.

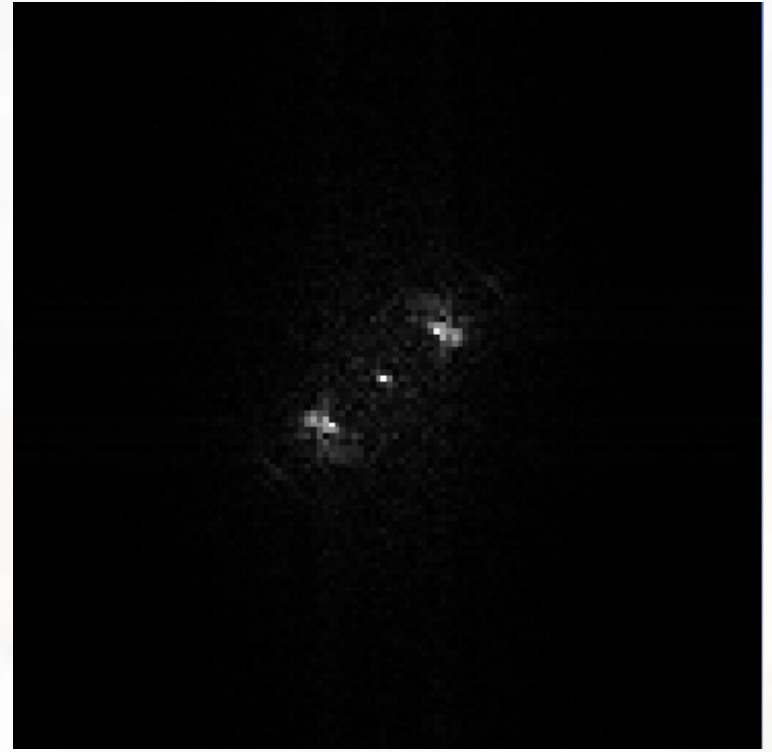
Frequency based method – Jain et. al (1999)

1. Frequency based approach convert the fingerprint image into the frequency space and perform the classification in that space.
2. In Jain et. al (1999), Gabor filters at 16 different orientation values are applied to different sectors of the fingerprint image. The Gabor coefficients form the feature for classification.

Fingerprint as Oriented Texture

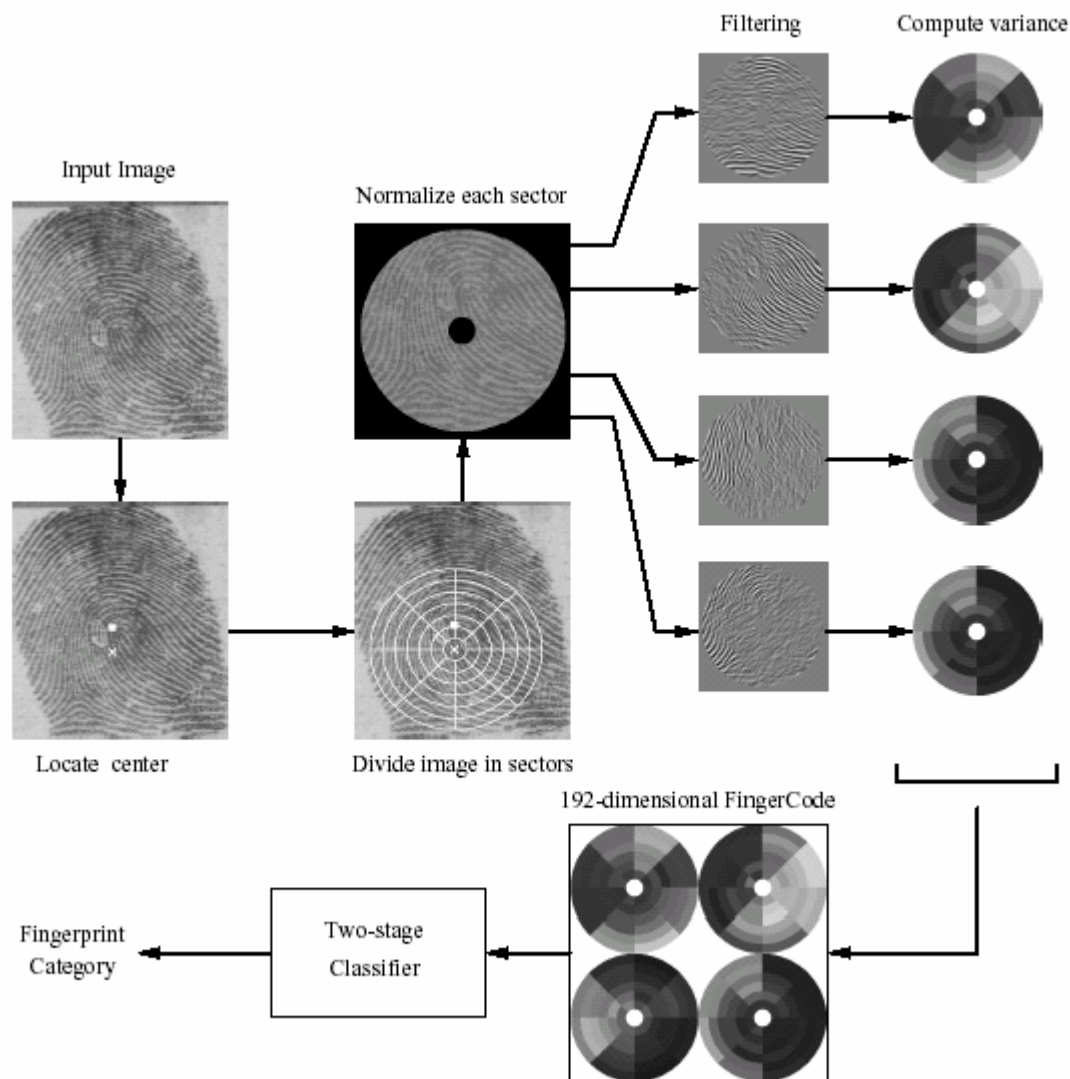


(a) Ridges in local region



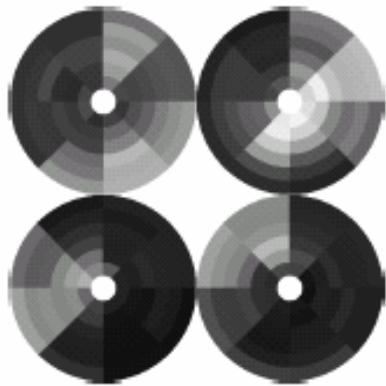
(b) Fourier spectrum of (a)

Fingerprint Classification Algorithm

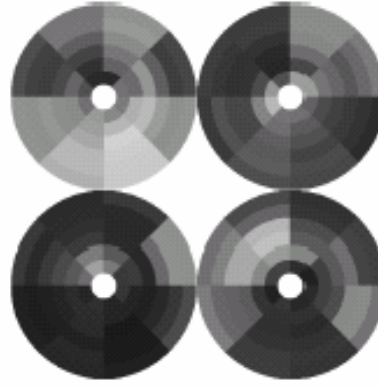


•A. K. Jain, S. Prabhakar and L. Hong, "[A Multichannel Approach to Fingerprint Classification](#)", *IEEE Transactions on PAMI*, Vol.21, No.4, pp. 348-359, April 1999.

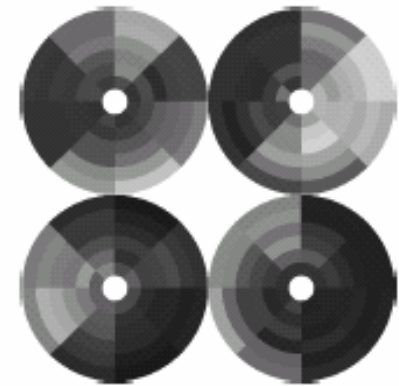
192-dimensional Feature Vector



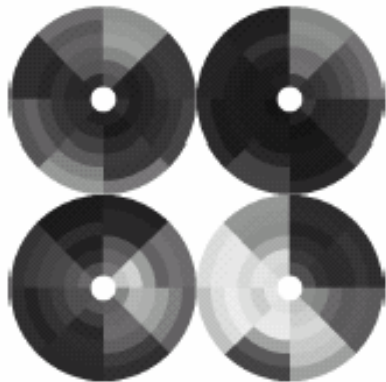
Test vector (Left Loop)



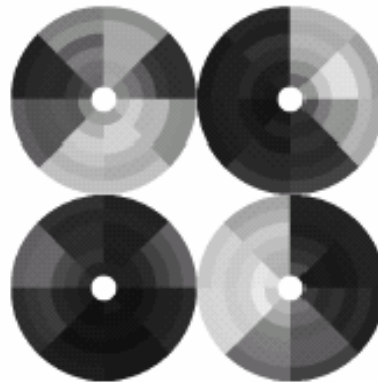
Whorl



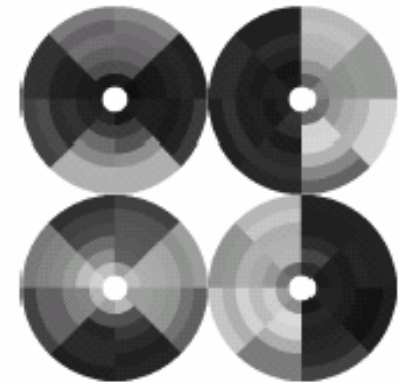
Right Loop



Left Loop



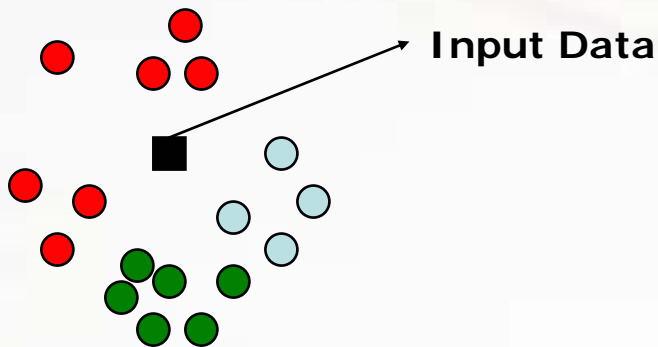
Arch



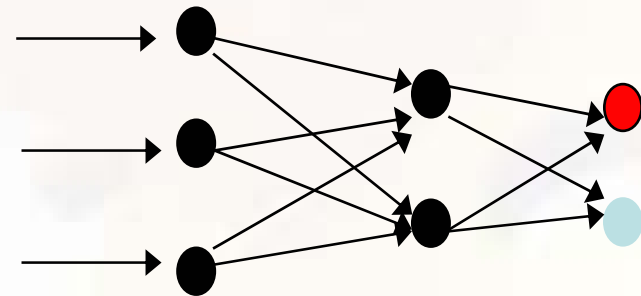
Tented Arch

Two-stage classifier

- K-nearest neighbor classifier
- Neural Network classifier



A K-NN Classifier

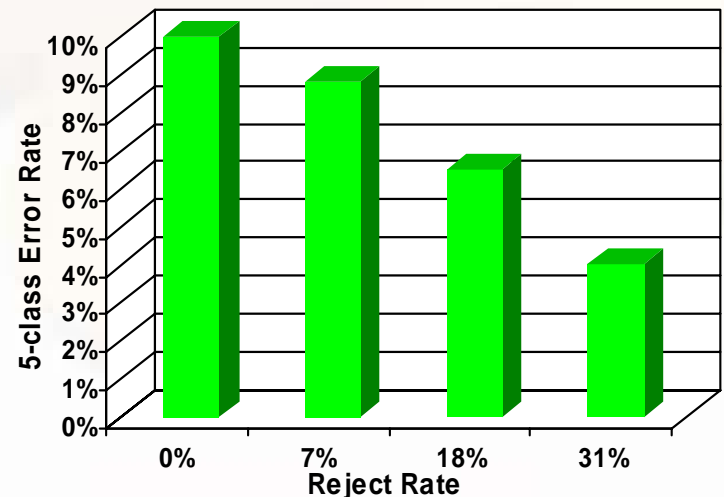


Neural Network Classifier

Classification Results

- Five-class classification error is 10%; error is 4% with 30.8% rejection rate.
- Four-class classification error is 5.2%; error is 2.2% with 30.8% rejection rate.

True Class	Assigned Class				
	Whorl	Right Loop	Left Loop	Arch	Tented Arch
Whorl	366	16	8	4	1
Right Loop	3	372	1	8	17
Left Loop	6	0	364	6	7
Arch	2	1	3	405	39
Tented Arch	0	6	14	55	261



Approaches based on mathematical models – Silviu & Jain, 2002

Class-specific kernels are defined: the kernel for the whorl class is the unit circle, and for the other classes, the kernels are defined via splines.



Figure: Kernels for (a) arch, (b) left-loop, (c) right-loop, and (d) whorl.

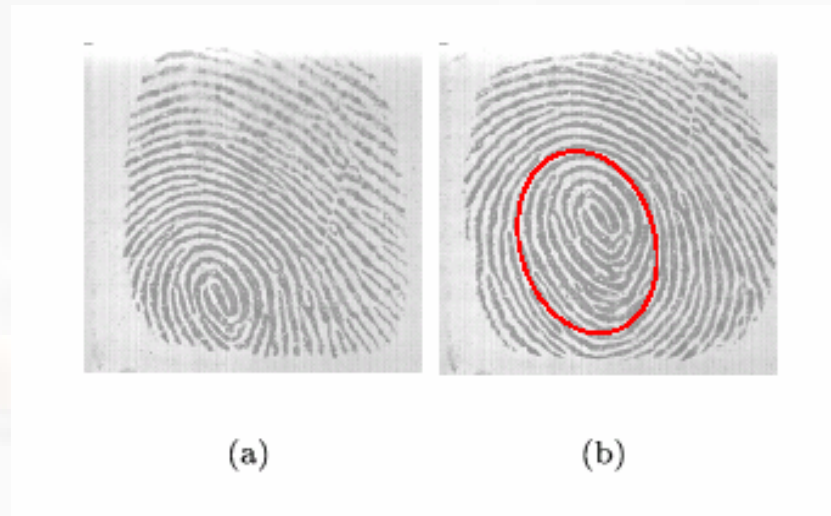
For a fingerprint image, the energy functional

$$E(\gamma) = \frac{\int_{\gamma} \sin^2(\alpha - \beta(\gamma)) d\gamma}{\int_{\gamma} d\gamma}$$

is minimized to determine the best fitting kernel.

Silviu & Jain (cont.)

Results of the fitting algorithm:



The best fitting kernel (the one that minimizes the energy functional below a certain threshold) is taken to be the class of the fingerprint image. Experimental results based on the NIST4 database yields a classification accuracy of 91.25% for the 4 class problem.

Why Another Fingerprint Classifier ?

Dass & Jain (2004)

+ Limitations of the existing approaches:

- + Ridges are subject to breaks and discontinuities due to noise
- + Singular points may be missed in some fingerprint images
- + Mathematical models are too rigid to represent all possible ridge variations

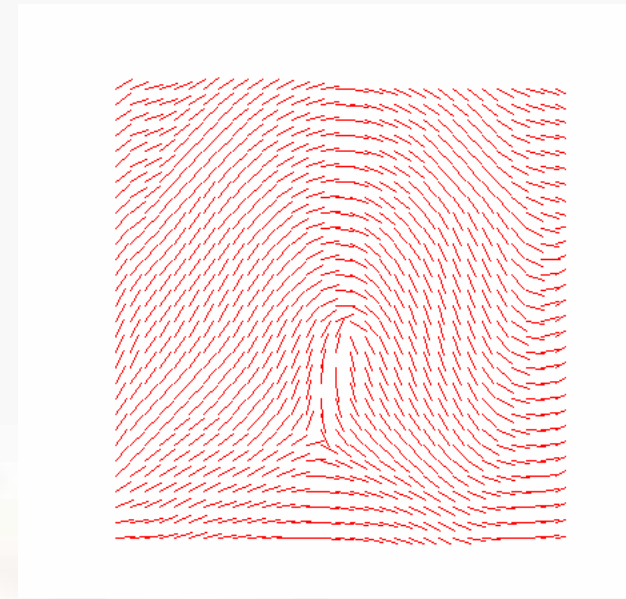
+ Requirements of a fingerprint classifier:

- + **Robust detection of global ridge characteristics**
- + Classification **invariance under affine transformations** and mild non-linear deformations of the fingerprint

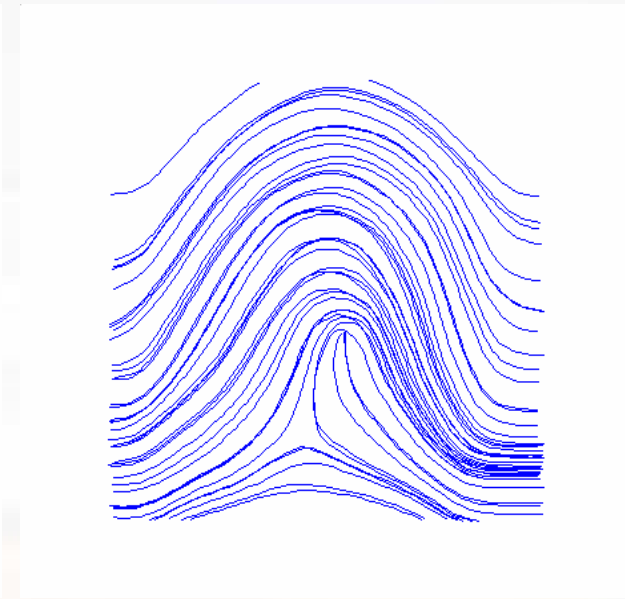
Orientation Field Flow Curves



Fingerprint Image



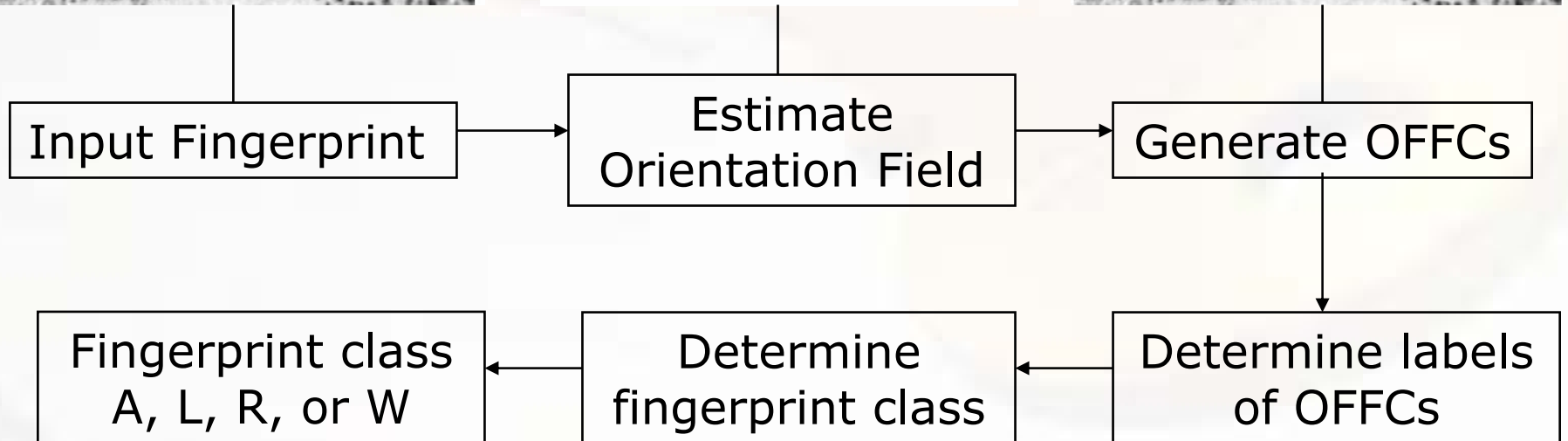
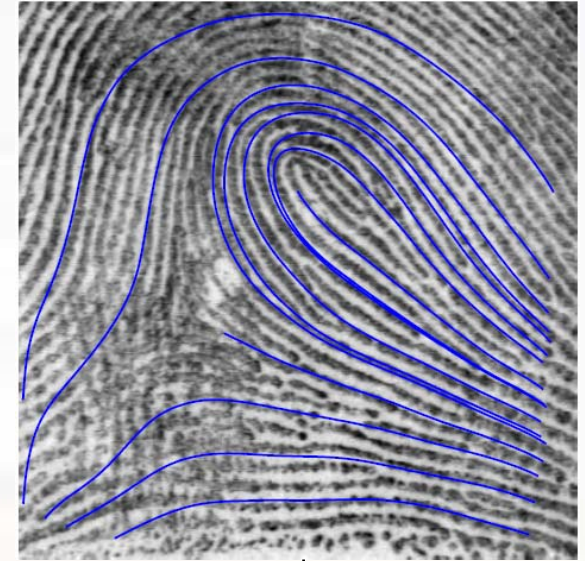
Orientation Field



Flow Curves

- **Orientation field** : local flow directions of the ridges and valleys
- Opposite flow directions are equivalent, angle $\in [-\pi/2, \pi/2]$
- **Orientation field flow curve** (OFFC) is a curve whose tangent direction at each point is parallel to the orientation field direction
- This is **not ridge tracing**; OFFCs are **pseudoridges**

Schematic Diagram of Classification

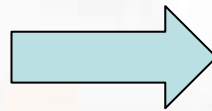


Estimation of Orientation Field*

A block-wise **squared gradient approach** with **smoothness prior** is used to obtain a smooth and robust estimate of orientation field



Input image



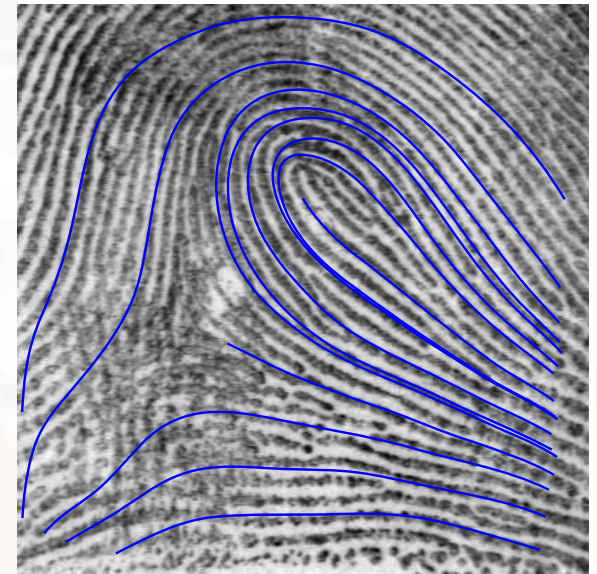
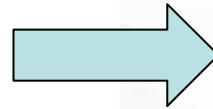
Orientation Field

* *S. C. Dass, "Markov Random Field Models for Directional Field and Singularity Extraction in Fingerprint Images", IEEE Transactions on Image Processing, October 2004*

Generation of Orientation Field Flow Curves (OFFCs)



Continuous
Orientation Field



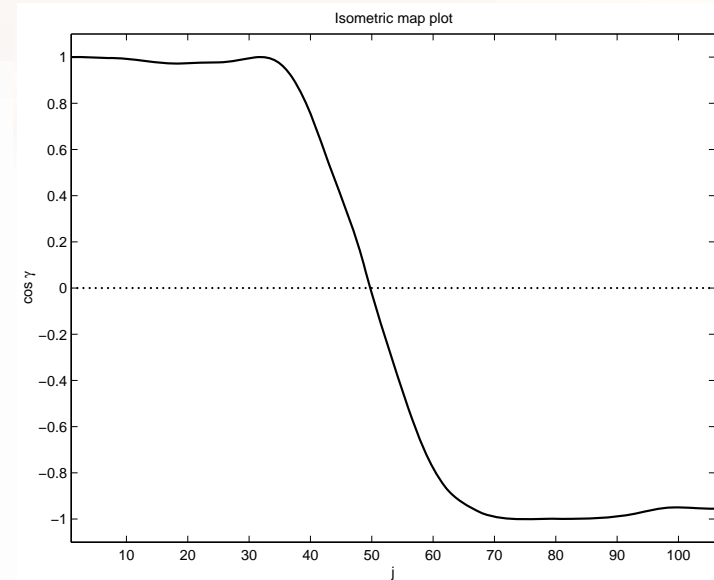
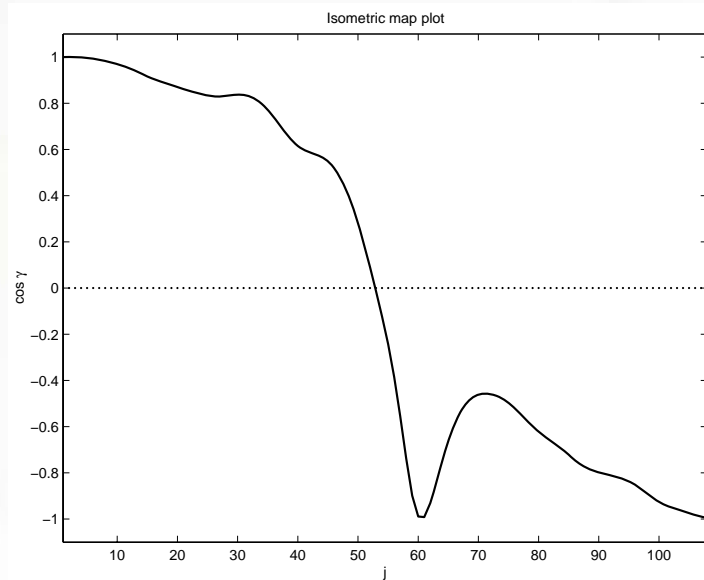
Orientation Field
Flow Curves

From a starting point s_0 , an OFFC is generated by tracing the paths from s_0 that is tangential to orientation field

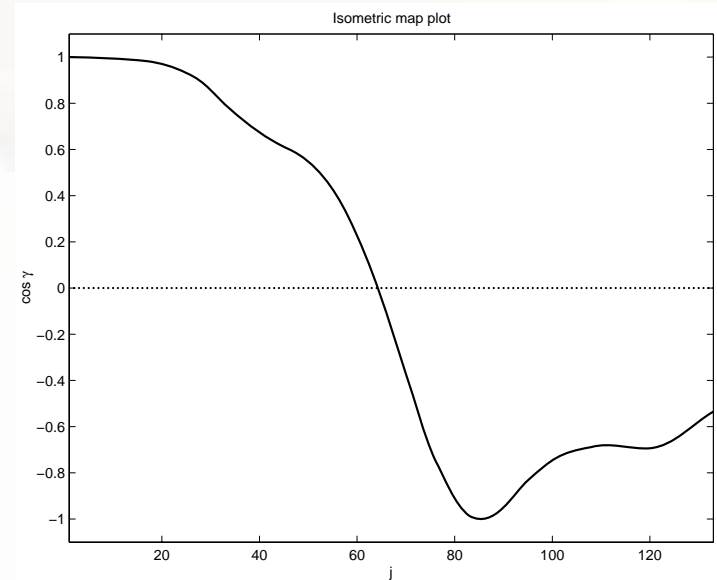
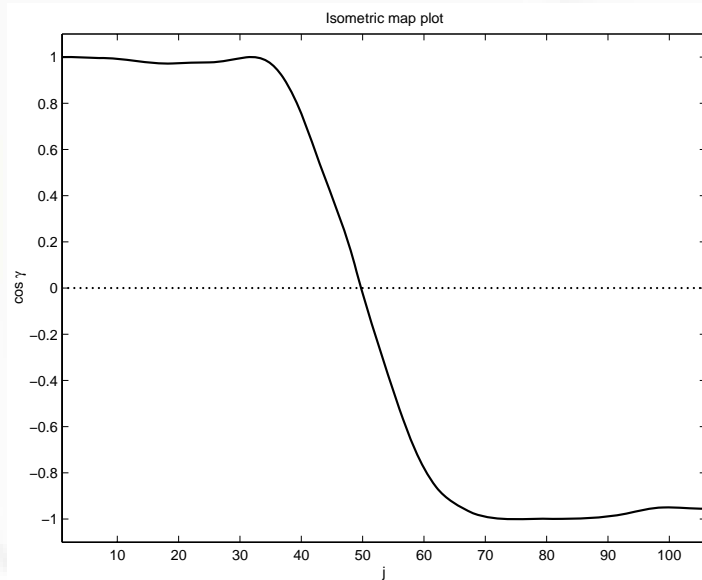
Detecting OFFC Type using Tangent Space Isometric Maps

- ✦ For each OFFC, we wish to determine whether it is a loop, arch or whorl
- ✦ The curve type can be identified using the tangent space isometric map of the OFFC
- ✦ Denote one end of the OFFC by s_e . Obtain the tangent plane at s_e , T_e
- ✦ For an intermediate point s on the OFFC, obtain the tangent plane at s , T_s
- ✦ Rotate T_e to match T_s ; say, the angle of rotation is θ_s
- ✦ The tangent space isometric map is the plot of $\cos(\theta_s)$ versus d_s , the distance of s from s_e along the OFFC

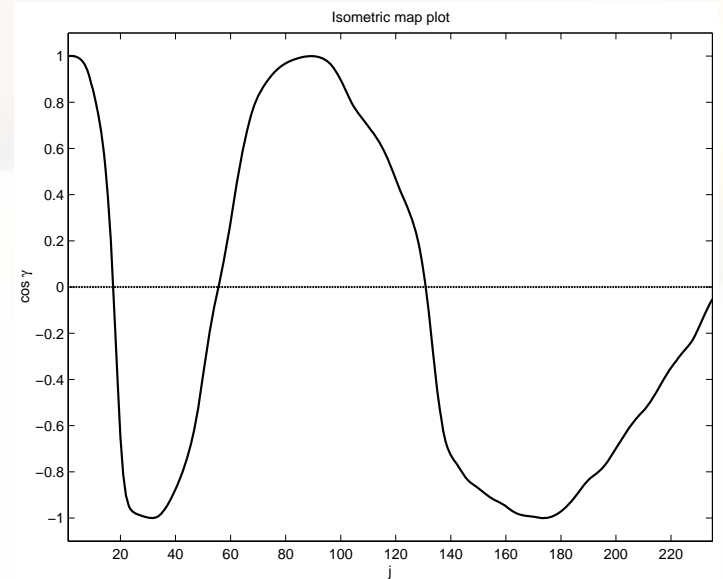
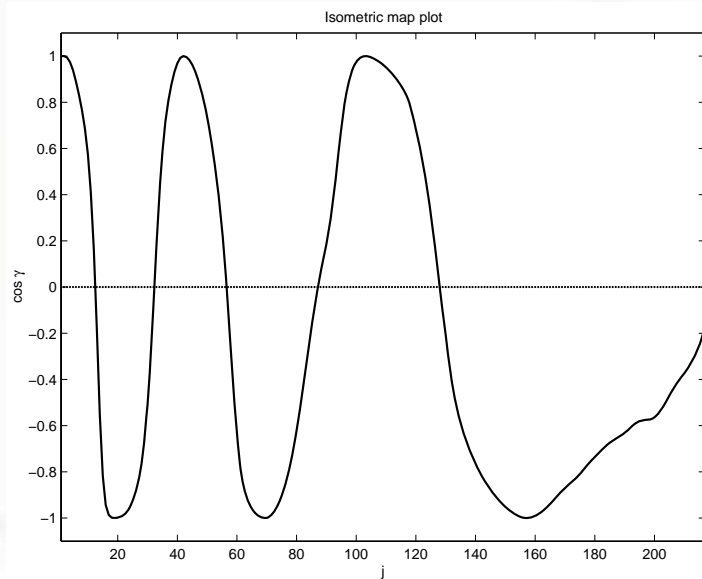
Tangent Space Maps of Left-Loop



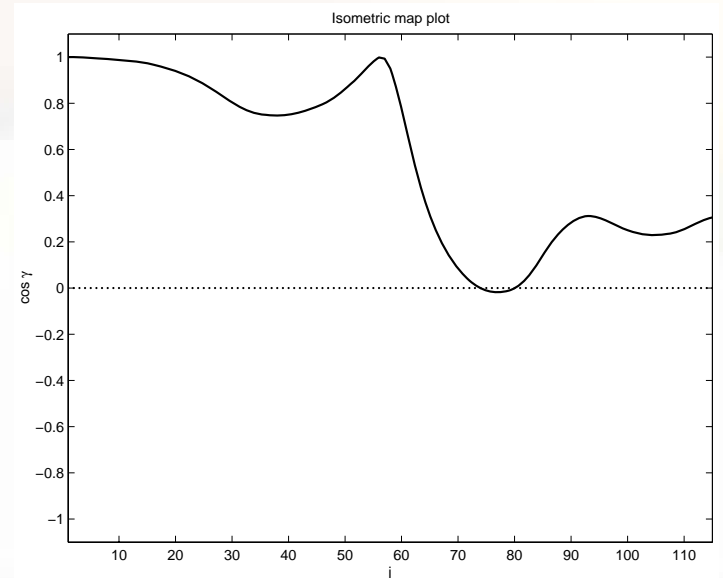
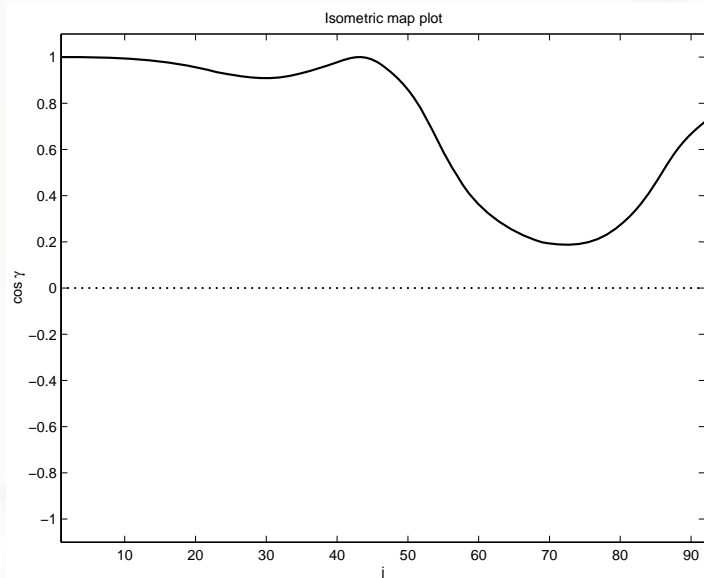
Tangent Space Maps of Right-Loop



Tangent Space Maps of Whorl



Tangent Space Maps of Arch



Tangent Space Isometries of OFFCs

- ✦ The **number of zero crossings**, and **values of local maxima and minima** between zero crossings are the salient features
- ✦ Left- and right-loops are differentiated based on sign changes $U_x * U_y$ of the tangent vector (U_x, U_y)
- ✦ Left-loops are characterized by sign transitions of from +1 to -1 and back to +1. Right-loops are characterized by sign transitions of from -1 to +1 and back to -1
- ✦ Note that these features are invariant to rotation, translation and scale

Fingerprint Classification Rules

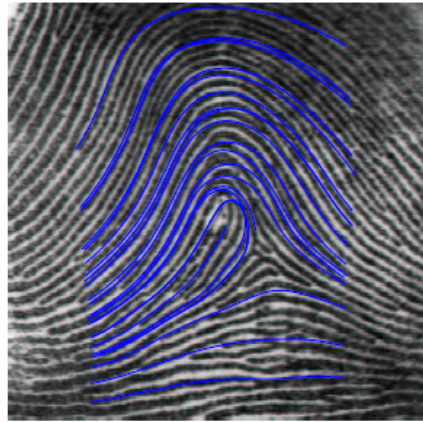
- ✦ Classify each OFFC as whorl, left-loop, right-loop or arch using the tangent space isometric maps
- ✦ Let N_w , N_l , N_r and N_a denote the number of OFFCs classified as whorl, left-loop, right-loop and arch
- ✦ Select thresholds λ_w , λ_l , and λ_r . The classification rule is
- ✦ If $N_w > \lambda_w$, classify as Whorl;
Else:
 - If $N_l > \lambda_l$ and $N_r \leq \lambda_r$, classify as Left-loop;
 - If $N_l \leq \lambda_l$ and $N_r > \lambda_r$, classify as Right-loop;
 - If $N_l \leq \lambda_l$ and $N_r \leq \lambda_r$, classify as Arch

Classification Results

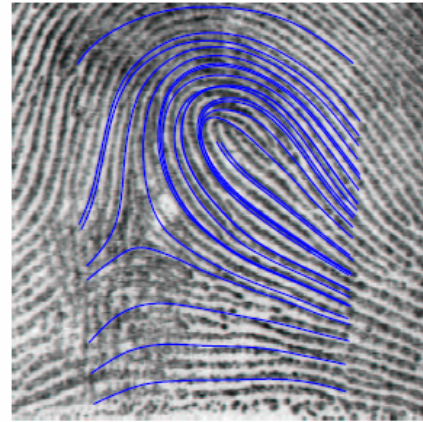
- ✦ Experiments were conducted on the NIST 4 fingerprint database containing 4,000 8-bit gray scale fingerprint images
- ✦ Select $\lambda_w = 2$, $\lambda_l = 2$ and $\lambda_r = 1$
- ✦ Classification into 4 classes yielded an accuracy of **94.4%**

	Assigned Class					
True class	A	L	R	W	total	accuracy
A	797	2	1	0	800	99.6%
T	781	19	0	0	800	97.2%
L	63	730	1	6	800	91.2%
R	75	4	720	1	800	90.0%
W	12	23	18	747	800	93.3%

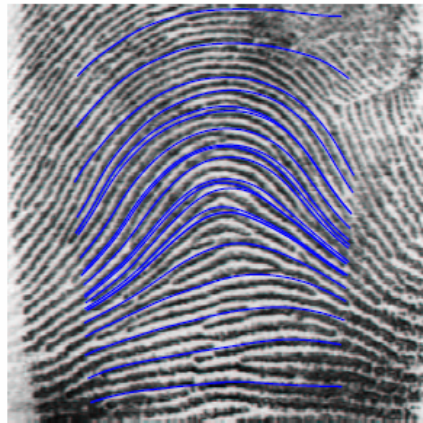
Examples of Correct Classifications



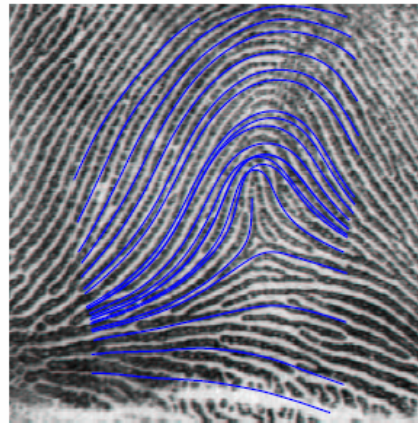
(a) left-loop



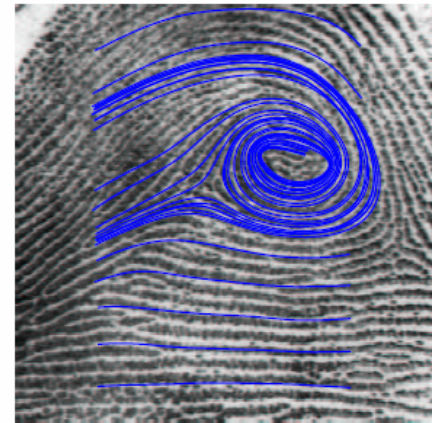
(b) right-loop



(c) plain arch

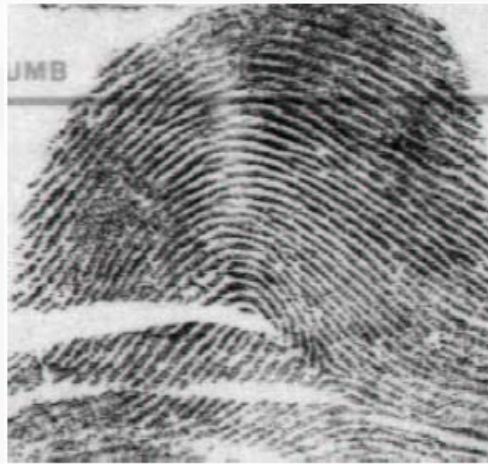


(d) tented arch

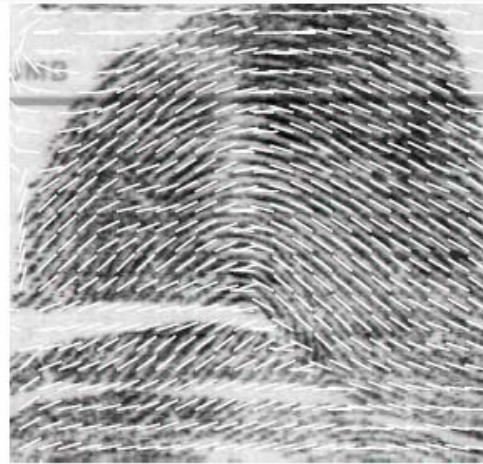


(e) whorl

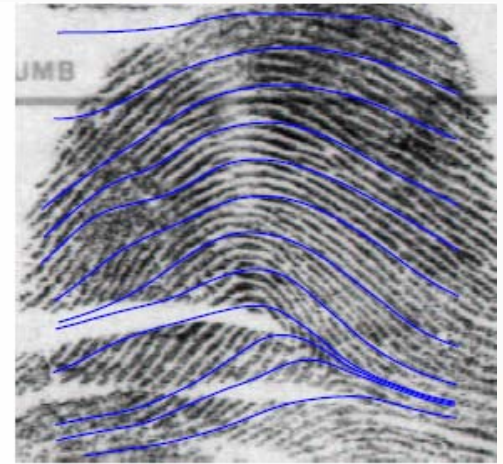
Sources of Classification Errors



(a) Input image



(b) Orientation field



(c) OFFCs

Oversmoothing of the orientation field

True class: L; Assigned class: A

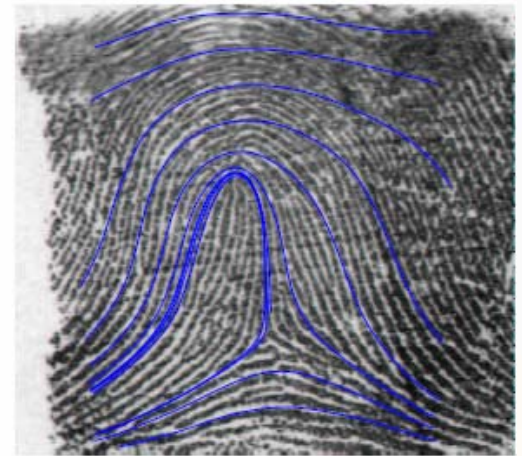
Sources of Classification Errors



(a) Input image



(b) Orientation field



(c) OFFCs

Detection of spurious loops

True class: A; Assigned class: L

Summary and Future Work

- ✦ We have proposed a fingerprint classification scheme based on the flow curves derived from the orientation field
- ✦ Performance of the proposed approach is comparable with the other state-of-the-art methods
- ✦ We plan to extend the 4-class classification to the 5- and 7-class problems by including other features of OFFCs into our classification procedure
- ✦ Other indexing techniques, besides the Henry system, will be investigated based on relevant features of the OFFCs